

# EEC3213: Optical Communications Photodetectors

## Problem Set

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**P1:** If the absorption coefficient of Si at wavelength of  $0.9\mu\text{m}$  is  $370\text{ cm}^{-1}$ . Determine the ratio of the optical power absorbed w.r.t. incident optical power  $P_0$  for depletion layer width of 1, 5, 10, 20 and  $50\mu\text{m}$  over the corresponding wavelength.

**P2:** If an optical power level  $P_0$  is incident on a photodiode, the electron hole-pair generated rate  $G(x)$  in the photodetector is given by

$$G(x) = \Phi_0 \alpha_s e^{-\alpha_s x}$$

Such that  $\Phi_0$  is the incident photos flux per unit area given by

$$\Phi_0 = \frac{P_0(1 - R_f)}{Ah\nu}$$

where A is the detector area. Show that the primary photocurrent generated in the depletion region of width  $w$  is given by

$$I_p = \frac{q}{h\nu} P_0(1 - R_f)(1 - e^{-\alpha_s w})$$

**P3:** Assuming that the value obtained in **P1** is a measurement of quantum efficiency. Determine the corresponding responsivity over that same wavelength of  $0.9\mu\text{m}$  assuming a  $20\mu\text{m}$  thick depletion layer and  $R_f = 0$ .

**P4:** If the low frequency gain  $M_0$  of an avalanche photodiode, for applied voltages near the breakdown voltage,  $V_B$ , can be approximated by

$$M_0 = \frac{I_M}{I_P} \simeq \frac{V_B}{nI_M R_M}$$

where  $I_M$  is the total multiplied current,  $R_M$  accounts for the photodiode series resistance and the load resistor and  $n$  is an exponential factor depends on the semiconductor material and its doping profile.

Show that the maximum value of  $M_0$  occurs at

$$M_{0,max} = \left( \frac{V_B}{nI_P R_M} \right)^{1/2}$$

**P5:** Consider a sinusoidally modulated optical signal  $P(t)$  of frequency  $\omega$ , modulation index  $m$ , and average power  $P_0$  given by

$$P(t) = P_0(1 + m \cos \omega t)^2$$

Show that when this optical signal falls on a photodetector, the mean-square signal current  $\langle i_s^2 \rangle$  generated consists of a dc (average) component  $I_P$  and a signal current  $i_p$  given by

$$\langle i_s^2 \rangle = I_P^2 + \langle i_p^2 \rangle = (R_0 P_0)^2 + \frac{1}{2} (m R_0 P_0)^2$$

where  $R_0$  is the responsivity.

**P6:** Consider an avalanche photodiode receiver that has the following parameters: dark current  $I_D = 1$  nA, leakage current  $I_L = 1$  nA, quantum efficiency  $\eta = 0.85$ , gain  $M = 100$ , excess noise factor  $F = M^{1/2}$ , load resistor  $R_L = 10^4 \Omega$ , and bandwidth  $B = 10$  KHz. Suppose a sinusoidally varying 850-nm signal having a modulation index  $m = 0.85$  falls on the photodiode, which is at room temperature ( $T = 300$  K). To compare the contributions from the various noise terms, compute the following various signal-to-noise components ratio:  $\left(\frac{S}{N}\right)_Q$ ,  $\left(\frac{S}{N}\right)_{DB}$ ,  $\left(\frac{S}{N}\right)_{DS}$  and  $\left(\frac{S}{N}\right)_T$  for this parameter set.

**P7:** For the parameter set in **P6**, if an average optical power level  $P_0 = -50$  dBm falls on the detector. Calculate the optimal value of  $M$  for maximum signal-to-noise ratio.

**P8:** Suppose we have a silicon *pin* photodiode which has a depletion layer width  $w = 20 \mu\text{m}$ , an area  $A = 0.05 \text{ mm}^2$ , and a dielectric constant  $K_s = 11.7$ . If the photodiode is to operate with a  $10 \text{ K}\Omega$  load resistor at 800 nm, where the absorption coefficient  $\alpha_s = 10^3 \text{ cm}^{-1}$  and the drift speed is limited to the hole speed of  $4.4 \times 10^6 \text{ cm/s}$ .

(a) Compare the RC time constant and the carrier drift time of the device?

(b) Is carrier diffusion time of importance in this photodiode?